



Similarity Learning with (or without) Convolutional Neural Network

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Image Source: Google



Outline – This Section

- Why do we need Similarity Measures
- Metric Learning as a measure of Similarity
 - Notion of a metric
 - Unsupervised Metric Learning
 - Supervised Metric Learning
- Traditional Approaches for Matching
- Challenges with Traditional Matching
 Techniques
- Deep Learning as a Potential Solution
- Application of Siamese Network for different tasks



Need for Similarity Measures

Several applications of Similarity Measures exists in today's world:



• Recognizing handwriting in checks.



• Automatic detection of faces in a camera image.



• Search Engines, such as Google, matching a **query** (could be text, image, etc.) with a set of **indexed documents** on the web.



- A **Metric** is a function that quantifies a "distance" between every pair of elements in a set, thus inducing a measure of similarity.
- A metric f(x,y) must satisfy the following properties for all x, y, z belonging to the set:
 - Non-negativity: $f(x, y) \ge 0$
 - Identity of Discernible: f(x, y) = 0 <=> x = y
 - *Symmetry*: f(x, y) = f(y, x)
 - Triangle Inequality: $f(x, z) \le f(x, y) + f(y, z)$



In broad strokes metrics are of two kinds:

Pre-defined Metrics: Metrics which are fully specified without the knowledge of data.

E.g. Euclidian Distance: $f(x, y) = (x - y)^T(x - y)$

• Learned Metrics: Metrics which can only be defined with the knowledge of the data.

E.g. Mahalanobis Distance: $f(x, y) = (x - y)^T M(x - y)$; where **M** is a matrix that is estimated from the data. Learned Metrics are of two types:

- Unsupervised : Use unlabeled data
- Supervised : Use labeled data



UNSUPERVISED METRIC LEARNING



- Mahalanobis Distance weighs the Euclidian distance between two points, by the standard deviation of the data.
 - f(x, y) = (x y)^TΣ⁻¹(x y); where Σ is the meansubtracted covariance matrix of all data points.



Chandra, M.P., 1936. On the generalised distance in statistics. In *Proceedings of the National Institute of Sciences of India* (Vol. 2, No. 1, pp. 49-55).



SUPERVISED METRIC LEARNING



Supervised Metric Learning

- In this setting, we have access to labeled data samples (z = {x, y}).
- The typical strategy is to use a 2-step procedure:
 - Apply some **supervised** domain transform.
 - Then use one of the unsupervised metrics for performing the mapping.



Bellet, A., Habrard, A. and Sebban, M., 2013. A survey on metric learning for feature vectors and structured data. *arXiv preprint arXiv:1306.6709*.

Linear Discriminant Analysis (LDA)

- In Fisher-LDA, the goal is to project the data to a space such that the ratio of "between class covariance" to "within class covariance" is maximized.
- This is given by: $J(w) = max_w (w^TS_Bw)/(w^TS_Ww)$



Fisher, R.A., 1936. The use of multiple measurements in taxonomic problems. *Annals of eugenics*, 7(2), pp.179-188.



TRADITIONAL MATCHING TECHNIQUES

The traditional approach for matching images, relies on the following pipeline:

- **1. Extract Features**: For instance, color histograms of the input images.
- Learn Similarity: Use L₁-norm on the features.

Stricker, M.A. and Orengo, M., 1995, March. Similarity of color images. In *IS&T/SPIE's Symposium on Electronic Imaging: Science & Technology* (pp. 381-392). International Society for Optics and Photonics.

The principal shortcoming of traditional metric learning based methods is that the **feature representation** of the data and the **metric** are **not learned jointly**.



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- Why do we need Similarity Measures
- Metric Learning as a measure of Similarity
- Traditional Approaches for Similarity Learning
- Challenges with Traditional Similarity Measures
- Deep Learning as a Potential Solution
 - Siamese Networks
 - Architectures
 - Loss Function
 - Training Techniques
- Application of Siamese Network to different tasks



CNNs can **jointly optimize** the representation of the input data conditioned on the "similarity" measure being used, aka end-toend learning.



Image Source: Google



- **Input**: Given a pair of input images, we want to know how "similar" they are to each other.
- **Output**: The output can take a variety of forms:
 - Either a binary label, i.e. 0 (same) or 1 (different).
 - A **Real** number indicating how similar a pair of images are.



Typical Siamese CNN

- Input: A pair of input signatures.
- Output (Target): A label, 0 for similar, 1 else.





Image Source: Google

Bromley, J., Bentz, J.W., Bottou, L., Guyon, I., LeCun, Y., Moore, C., Säckinger, E. and Shah, R., 1993. Signature Verification Using A "Siamese" Time Delay Neural Network. *IJPRAI*, 7(4), pp.669-688.



SIAMESE CNN - ARCHITECTURE

Standard architecture of Siamese CNN



Simo-Serra, E., Trulls, E., Ferraz, L., Kokkinos, I., Fua, P. and Moreno-Noguer, F., 2015. Discriminative learning of deep convolutional feature point descriptors. In *Proceedings of the IEEE International Conference on Computer Vision* (pp. 118-126).



- No one "architecture" fits all!
- Design largely governed by what performs well empirically on the task at hand.



Zagoruyko, S. and Komodakis, N., 2015. Learning to compare image patches via convolutional neural networks. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition* (pp. 4353-4361).



TRIPLET NETWORK



D(f(A), f(B)) < D(f(A), f(C))

- Compare triplets in one go.
- Check if the sample in the **topmost** channel, is more similar to the one in the middle or the one in the bottom.
- Allows us to learn ranking between samples.

Vo, N.N. and Hays, J., 2016, October. Localizing and orienting street views using overhead imagery. In European Conference on Computer Vision (pp. 494-509).



SIAMESE CNN – LOSS FUNCTION





Similar images

- Is there a problem with this formulation?
 - Yes.
 - The model could learn to embed every input to the same point, i.e. predict a constant as output.
 - In such a case, every pair of input would be categorized as a positive pair.

Chopra, S., Hadsell, R. and LeCun, Y., 2005, June. Learning a similarity metric discriminatively, with application to face verification. In *Computer Vision and Pattern Recognition, 2005. CVPR 2005. IEEE Computer Society Conference on* (Vol. 1, pp. 539-546). IEEE.



Siamese CNN – Loss Function





$L = \Sigma loss$ of positive pairs + $\Sigma loss$ of negative pairs

Chopra, S., Hadsell, R. and LeCun, Y., 2005, June. Learning a similarity metric discriminatively, with application to face verification. In *Computer Vision and Pattern Recognition, 2005. CVPR 2005. IEEE Computer Society Conference on* (Vol. 1, pp. 539-546). IEEE.



- We can use different loss functions for the two types of input pairs.
- Typical positive pair (x_p, x_q) loss: $L(x_p, x_q) = ||x_p x_q||^2$ (Euclidian Loss)



Bell, S. and Bala, K., 2015. Learning visual similarity for product design with convolutional neural networks. ACM *Transactions on Graphics (TOG)*, 34(4), p.98.



Siamese CNN – Loss Function

• Typical negative pair (x_n, x_q) loss : $L(x_n, x_q) = max(0, m^2 - ||x_n - x_q||^2)$ (Hinge Loss)



Bell, S. and Bala, K., 2015. Learning visual similarity for product design with convolutional neural networks. ACM *Transactions on Graphics (TOG)*, 34(4), p.98.



Choices of Loss Function

- Several choices for the Loss Functions are available. Choice depends on the task at hand.
- Loss Functions for **2-Stream Networks**:
 - Margin Based:
 - Contrastive Loss: Loss(x_p, x_q, y) =
 - $y * ||x_p x_q||^2 + (1 y) * max(0, m^2 ||x_p x_q||^2)$
 - Allows us to learn a margin of separation.
 - Extensible for Triplet Networks
 - Non-Margin Based:
 - Distance-Based Logistic Loss:

 $P(x_{p}, x_{q}) = (1 + \exp(-m))/(1 + \exp(||x_{p} - x_{q}|| - m))$ Loss(x_p, x_q, y) = LogLoss(P(x_p, x_q), y)

• Good for quicker convergence.



Choices of Loss Function

• Contrastive Loss:

For similar samples: Loss(x_p, x_q) = $||x_p-x_q||^2$



- Distance-Based Logistic Loss:
- For similar pairs

 $P(x_{p}, x_{q}) = (1 + \exp(-m))/(1 + \exp(||x_{p} - x_{q}|| - m)) \rightarrow 1 \text{ quickly}$ $Loss(x_{p}, x_{q}, y) = LogLoss(P(x_{p}, x_{q}), y)$

Vo, N.N. and Hays, J., 2016, October. Localizing and orienting street views using overhead imagery. In European Conference on Computer Vision (pp. 494-509).



SIAMESE CNN – TRAINING



• Update each of the two streams independently and then average the weights.



- Does this technique remind us of anything?
 - Training in RNNs.
- Data augmentation may be used for more effective training.
 - Typically we hallucinate more examples by performing random crops, image flipping, etc.



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- Deep Learning as a Potential Solution
- Application of Siamese Network to different tasks
 - Generating invariant and robust descriptors
 - Person Re-Identification
 - Rendering a street from Different Viewpoints
 - Newer nets for Person Re-Id, Viewpoint Invariance and Multimodal Data.
 - Use of Siamese Networks for Sentence Matching



APPLICATIONS

Discriminative Descriptors for Local Patches



Learn a discriminative representation of patches from different views of 3D points

Simo-Serra, E., Trulls, E., Ferraz, L., Kokkinos, I., Fua, P. and Moreno-Noguer, F., 2015. Discriminative learning of deep convolutional feature point descriptors. In *Proceedings of the IEEE International Conference on Computer Vision* (pp. 118-126).

Deep Descriptor



$$l(x_1, x_2) = \begin{cases} ||D(x_1) - D(x_2)||_2, & p_1 = p_2 \\ \max\left(0, C - ||D(x_1) - D(x_2)||_2\right), & p_1 \neq p_2 \end{cases}$$

Use the CNN outputs of our Siamese networks as descriptor

Simo-Serra, E., Trulls, E., Ferraz, L., Kokkinos, I., Fua, P. and Moreno-Noguer, F., 2015. Discriminative learning of deep convolutional feature point descriptors. In *Proceedings of the IEEE International Conference on Computer Vision* (pp. 118-126).



Evaluation

Comparison of area under precision-recall curve

Dataset	SIFT (Non-deep)	[23](Non-deep)	Ours
ND	0.346	0.663	0.667
ТО	0.425	0.709	0.545
LY	0.226	0.558	0.608
All	0.370	0.693	0.756

SIFT: hand-crafted features

[23]: descriptor via convex optimization



Simo-Serra, E., Trulls, E., Ferraz, L., Kokkinos, I., Fua, P. and Moreno-Noguer, F., 2015. Discriminative learning of deep convolutional feature point descriptors. In *Proceedings of the IEEE International Conference on Computer Vision* (pp. 118-126).



Person Re-Identification



CUHK03 Dataset




Are they the same person?









Person Re-Identification



True

positive

True negative

























Tied Convolution

- Use convolutional layers to compute higher-order features
- Shared weights



Cross-Input Neighborhood Differences

 Compute *neighborhood difference* of two feature maps, instead of elementwise difference.

Example: f, g are feature maps of two input images





Cross-Input Neighborhood Differences

 Compute *neighborhood difference* of two feature maps, instead of elementwise difference.

Example: f, g are feature maps of two input images





Cross-Input Neighborhood Differences

- Compute *neighborhood difference* of two feature maps, instead of elementwise difference.
- A neighborhood-patch size of 5 was used in the paper:

 $K_{i}(x,y)=f_{i}(x,y)I(5,5)-N[g_{i}(x,y)]$ where I(5,5) is a 5x5 matrix of 1s, $N[g_{i}(x,y)] \text{ is the 5x5 neighborhood of}$ $g_{i} \text{ centered at } (x,y)$

 Another neighborhood difference map K' was also computed where f and g were revised.





Patch Summary Features

- Convolutional layers with 5x5 filters and stride 5 (the size of neighborhood patch).
- Provides a high-level summary of the crossinput differences in a neighborhood patch.





Across-Patch Features

- Convolutional layers with 3x3 filters and stride 1.
- Learn spatial relationships across neighborhood differences





Across-Patch Features

- Fully connected layer.
- Combine information from patches that are far from each other.
- Output: 2 softmax units



Visualization of Learned Features





Evaluation

Method	Elementwise Difference	Neighborhood Difference
Identification rate	27.66%	54.74%

Method	Regular Siamese Network	This work	
Identification rate	42.19%	54.74%	















Which one is the correct match?





Classification CNN:



L(A, B, l) = LogLossSoftMax(f(I), l)

I = concatenation(A, B) f = AlexNet $l = \{0, 1\}, label$



Classification CNN:



L(A, B, l) = LogLossSoftMax(f(I), l)

I = concatenation(A, B)f = AlexNet $l = \{0, 1\}, label$

Siamese-like CNN:



L(A, B, l) = l * D + (1 - l) * max(0, m - D)

 $D = //f(A) - f(B)//_{2}$ m = margin parameter



Classification CNN:



L(A, B, l) = LogLossSoftMax(f(I), l)



Siamese-like CNN:



L(A, B, l) = l * D + (1 - l) * max(0, m - D)

 $D = //f(A) - f(B)//_{2}$ m = margin parameter

Siamese-classification hybrid network:



$L(A, B, l) = LogLossSoftMax(f_{fc}(I_{conv}), l)$

 $I_{conv} = concatenation(f_{conv}(A), f_{conv}(B))$



Classification CNN:



L(A, B, l) = LogLossSoftMax(f(I), l)

I = concatenation(A, B)f = AlexNet $l = \{0, 1\}, label$

Siamese-like CNN:



L(A, B, l) = l * D + (1 - l) * max(0, m - D)

 $D = //f(A) - f(B)//_{2}$ m = margin parameter

Siamese-classification hybrid network:



$L(A, B, l) = LogLossSoftMax(f_{fc}(I_{conv}), l)$

 $I_{conv} = concatenation(f_{conv}(A), f_{conv}(B))$



L(A, B, C) = max(0, m + D(A, B) - D(A, C))

(A, B) is a match pair(A, C) is a non-match pair



Distance-based Logistic Loss

$$p(A,B) = \frac{1 + exp(-m)}{1 + exp(D-m)}$$
$$L(A, B, l) = LogLoss (p(A, B), l)$$

where $D = //f(A) - f(B)//_2$ m = margin parameter



Matched/Nonmatched instances are pushed away from the "boundary" in the inward/outward direction.

Performance of Different Networks

Matching accuracy

Test set	Denver	Detroit	Seattle
Siamese	85.6	83.2	82.9
Triplet	88.8	86.8	86.4

Siamese-like CNN:

Triplet network CNN:





Observation 1:

• Triplet network outperforms the Siamese by a large margin

Performance of Different Networks

Matching accuracy

Test set	Denver	Detroit	Seattle	
Siamese	85.6	83.2	82.9	
Siamese-DBL	90.0	88.0	88	
Triplet	88.8	86.8	86.4	
Triplet-DBL	90.2	88.4	87.6	

Siamese-like CNN:



Triplet network CNN:



Distance-based logistic (DBL) loss:

$$p(A,B) = \frac{1 + exp(-m)}{1 + exp(D-m)}$$
$$L(A, B, l) = LogLoss(p(A, B), l)$$

Observation 2:

• Distance-based logistic (DBL) Nets significantly outperform the original network.

Performance of Different Networks

Matching accuracy

Test set	Denver	Detroit	Seattle
Siamese Net	85.6	83.2	82.9
Triplet Net	88.8	86.8	86.4
Classification Net	90.0	87.8	87.7
Hybrid Net	91.5	88.7	89.4

Siamese-like CNN:









Classification-siamese hybrid:



Observation 3:

- Classification networks achieved better accuracy than Siamese and triplet networks.
- Jointly extract and exchange information from both input images.



MORE VARIANTS OF SIAMESE CNNs



SIAMESE CNN – INTERMEDIATE MERGING



- Combining at an **intermediate stage** allows us to capture patch-level variability.
- Performing inexact (soft) matching yields superior performance. Match(X, Y) = $(X-\mu_X)(Y-\mu_Y)/\sigma_X\sigma_Y$

Subramaniam, A., Chatterjee, M. and Mittal, A., 2016. Deep Neural Networks with Inexact Matching for Person Re-Identification. In *Advances in Neural Information Processing Systems* (pp. 2667-2675).



SIAMESE CNN – INTERMEDIATE MERGING Results:

• Handling Partial Occlusion:



Subramaniam, A., Chatterjee, M. and Mittal, A., 2016. Deep Neural Networks with Inexact Matching for Person Re-Identification. In *Advances in Neural Information Processing Systems* (pp. 2667-2675).

SIAMESE CNN – FOR VIEWPOINT INVARIANCE



Viewpoint invariance is incorporated by considering the similarity of response across the individual streams.

Kan, M., Shan, S. and Chen, X., 2016. Multi-view deep network for cross-view classification. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition* (pp. 4847-4855).



SIAMESE CNN – FOR VIEWPOINT INVARIANCE

Results on the CMU MultiPIE Dataset, for recognition across 7 poses.

Methods	-45 deg	-30 deg	-15 deg	15deg	30 deg	45 deg
CCA	0.73	0.96	1.00	0.99	0.96	0.69
KCCA (RBF)	0.80	0.98	0.99	1.00	0.98	0.72
FIP+LDA	0.93	0.96	1.00	0.99	0.96	0.90
MVP+LDA	0.93	1.00	1.00	1.00	0.99	0.96
Proposed	0.99	0.99	1.00	1.00	0.99	0.98

Kan, M., Shan, S. and Chen, X., 2016. Multi-view deep network for cross-view classification. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition* (pp. 4847-4855).

TWO STREAM CNN – FOR CROSS-MODAL EMBEDDING



Two stream networks have also been used for cross-modal embedding tasks. Here inputs from different modalities are mapped to a common space.

Wang, L., Li, Y. and Lazebnik, S., 2016. Learning deep structure-preserving image-text embeddings. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition* (pp. 5005-5013).



Application: Sentence completion, response to tweet, paraphrase identification





DEMO OF SIAMESE NETWORK



Demo: Architecture

MNIST Digit Similarity Assessment





Demo: Results



Code: @ywpkwon


- Quantifying "similarity" is an essential component of data analytics.
- Deep Learning approaches, such as "Siamese" Convolution Neural Nets, have shown promise recently.
- Several variants of Siamese CNN are available for making our life easier for a variety of tasks.



Reading List

- Bell, Sean, and Kavita Bala, <u>Learning visual similarity for product design with convolutional</u> <u>neural networks</u>, ACM Transactions on Graphics (TOG), 2015
- Chopra, Sumit, Raia Hadsell, and Yann LeCun, <u>Learning a similarity metric discriminatively</u>, <u>with application to face verification</u>, CVPR 2005
- Zagoruyko, Sergey, and Nikos Komodakis, <u>Learning to compare image patches via</u> <u>convolutional neural networks</u>, CVPR 2015
- Hoffer, Elad, and Nir Ailon, <u>Deep metric learning using triplet network</u>, arXiv:1412.6622
- Simo-Serra, Edgar, et al., <u>Discriminative Learning of Deep Convolutional Feature Point</u> <u>Descriptors</u>, ICCV 2015
- Vo, Nam N., and James Hays, <u>Localizing and Orienting Street Views Using Overhead Imagery</u>, ECCV 2016
- Ahmed, Ejaz, Michael Jones, and Tim K. Marks, <u>An Improved Deep Learning Architecture for</u> <u>Person Re-Identification</u>, CVPR 2015
- Hu, Baotian, et al., <u>Convolutional neural network architectures for matching natural language</u> <u>sentences</u>, NIPS 2014
- Kulis, Brian, Metric learning: A survey, Foundations and Trends in Machine Learning, 2013
- Su, Hang, et al., <u>Multi-view convolutional neural networks for 3d shape recognition</u>, ICCV 2015
- Zheng, Yi, et al., <u>Time Series Classification Using Multi-Channels Deep Convolutional Neural</u> <u>Networks</u>, WAIM 2014
- Yi, Kwang Moo, et al., <u>LIFT: Learned Invariant Feature Transform</u>, arXiv:1603.09114
- Stricker, M.A. and Orengo, M. <u>Similarity of color images</u>. In *IS&T/SPIE's Symposium on Electronic Imaging: Science & Technology* (pp. 381-392), 1995.



Appreciate your kind attention!